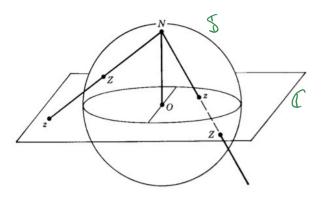
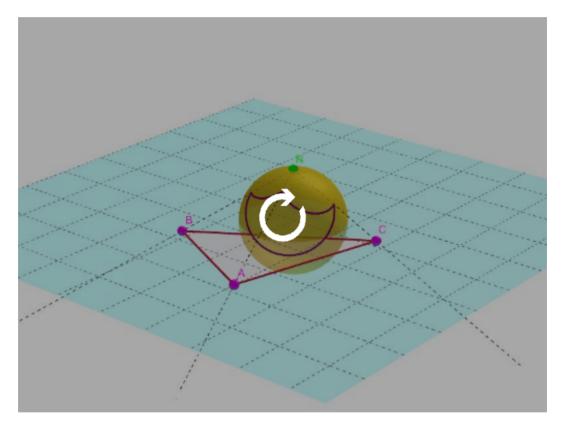
Stereographic projection

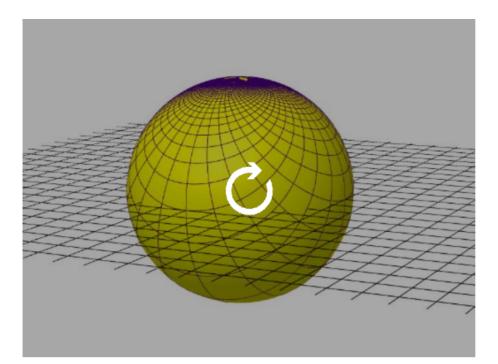
Wednesday, August 23, 2023 9:02 AM

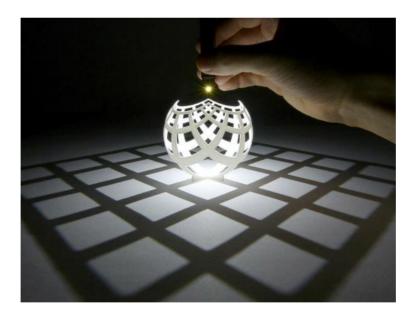


Stereographic projection



Stereographic Projection of Coordinate Grid to Sphere





N
$$Z = X + iy$$

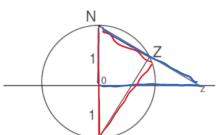
(X. X.) - $\lambda(X.y.)$ $\lambda = ?$

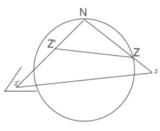
Complex Numbers Page 2

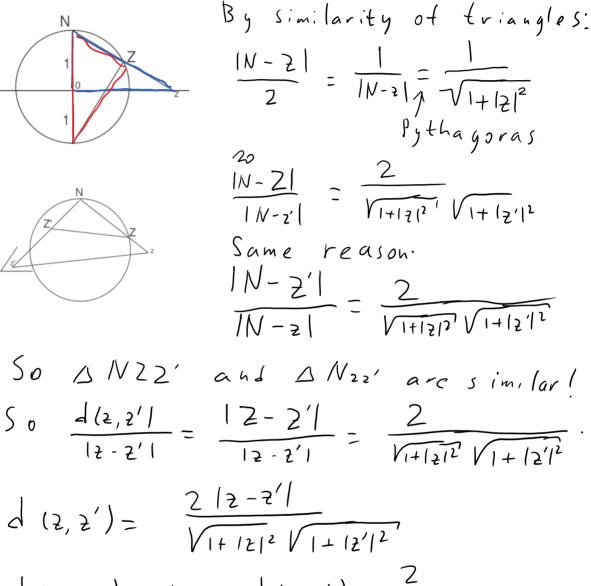
$$X_{1} = (1 - X_{3}) \times = \frac{2x}{12|^{2} + 1} = \frac{2 e_{2}}{|2|^{2} + 1} = X_{1}$$

$$X_{2} = \frac{2 I m t}{|t|^{2} + 1}$$

$$Z = \frac{X_{1} + i X_{2}}{|-X_{3}|^{2}}$$







$$|Z-M| = d(2, \infty) = \lim_{z' \to \infty} d(2, z') = \frac{z}{V_{1+|z|^2}}$$

Bonus (+1 p-1):
$$\widetilde{d}(2,2') = dist_{spherical}(2,2') = 7$$

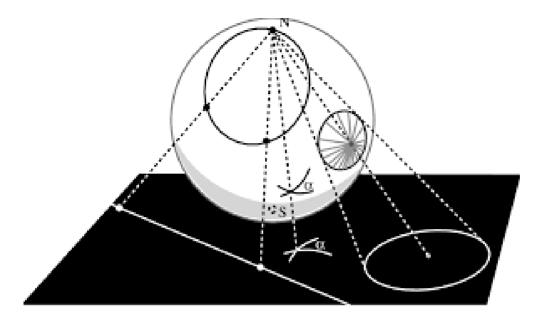
(in terms of $2,2'$).

Circles and straight lines on C are mapped to circles.

Proof. For straight line: the image is the intersection

Complex Numbers Page 5

For straight line: the image is the intersection of the sphere S with the plane through the line and N: a circle through N!



$$\frac{(ircle: computation:}{(X-a)^2 + (y-b)^2 = r^2}$$
Substitute by formula: $\binom{X}{y} = \frac{1}{1-X_3} \binom{X_1}{X_2}$
 $ax_1 + bx_2 + \frac{1+r^2 - a^2 - b^2}{2} x_3 = \frac{a^2 + b^2 - r^2 \cdot 1}{2} - equation of$
So, again, the image is plane intersected with $5!$
And any plane intersecting 5 and not through N
is of this form!

Can be done geometrically: see

Proof (stereographic projection proof that circles on the sphere project to circles in the plane)

